

二次元滑走板の境界条件について
(浸水長の変化に対応する解)

1. 序

I. 定常問題.

1.1 運動ポテンシャル等. 節 B.5, 2. 隣接

1.2 解核 I, B.9. の展開

1.3 浸水長の変化

1.4 解について.

II. 動揺問題.

1.1 運動ポテンシャル等.

1.2 解核.

1.3 浸水長の変化 (I) 力の無い場合
振動壁との比較

1.4 " (2)

1.5 解について.

特異各次解

昭和 年 月 日

1. 定常置 ^岸 $\gamma=0$
2. 動搖滑走板
3. 振動置

4. 滑走板 ($\gamma=0$) Wagner,
動搖.

5. 動搖滑走板 ($\gamma \neq 0$)

特異各次解

7月

2次元 滑走板

8月

3次元 "

~~逆時間ホロシナル~~

1. 近似3次元

近似解

mmmm

Bioplinghoff Ashley, Halfman
Aeroelasticity

chap 5 p. 188 - 293
4 7 380 - 420

$$(1 - \frac{c}{2})$$

$$f = f(x)$$

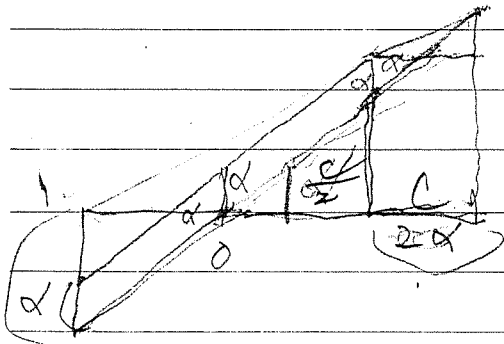
$$\frac{d}{dt} + U \frac{\partial}{\partial x}$$

$$e^{i\omega t} \frac{d}{dt} + U \frac{\partial}{\partial x}$$

$$v = \left(\frac{d}{dt} + U \frac{\partial}{\partial x} \right) (h + \rho x + \frac{5}{2} x^2)$$

$$= U \alpha f_x +$$

$$v \cdot w = \sum_{n=-\infty}^{\infty} v_n w_{m-n} e^{i\omega t}$$



$$(v \cdot w)_\alpha = \sum v_n w_{1-n} = v_0 w_1 + v_1 w_0 + \dots$$

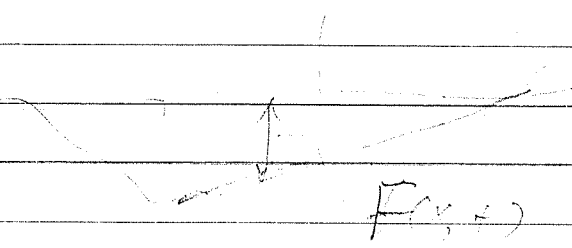
$$c = 2\alpha + \frac{\partial}{\partial c} \alpha$$

$$\frac{\alpha'}{1 + \frac{c}{2}} = \alpha$$

$$c = \frac{2\alpha}{1 - 2\frac{\partial}{\partial c} \alpha}$$

$$\left(1 + \frac{c}{2}\right) \alpha' = \frac{c}{2}$$

α



$$F(x, t)$$

$$f = f(x)$$

$$y = F(x, t) = h e^{i\omega t} + \theta x e^{i\omega t} + s \int_x f(x) e^{i\omega t}$$

$$\frac{D}{Dt}(y - F) = 0 \quad \left| \begin{array}{l} F_t = i\omega F \\ F_x = \end{array} \right.$$

$$\frac{\partial}{\partial t} v = -\frac{\partial}{\partial t} F - U \frac{\partial}{\partial x} F + v = 0$$

$$\phi = v = (i\omega F - (i\omega - U \frac{\partial}{\partial x}) \{ h + \theta x + s \int_x \})$$

$$\eta = \bar{\Phi} = h + \theta x + s \int_x$$

$$\int_0^{\infty} \frac{e^{ikx}}{k - k + \mu i} dk \quad x \rightarrow +\epsilon \quad -\frac{\pi i}{2} - \log(k|x|)$$

$$x \rightarrow -\epsilon \quad -\frac{3\pi i}{2} - \log(k|x|)$$

$$\int_0^{\infty} \frac{e^{-ikx}}{k + \beta} dk = e^{i\beta x} \int_{\beta}^{\infty} \frac{e^{-iux}}{u} du \quad u = \frac{t}{\beta} \quad x > 0.$$

$$= e^{i\beta x} \int_{\beta x}^{\infty} \frac{e^{-it}}{t} dt \quad \text{for } x > 0.$$

$$= e^{i\beta x} \int_{\beta|x|}^{\infty} \frac{e^{-it}}{t} dt \quad u = -\frac{t}{\beta} = \frac{t}{|\beta|} \quad \text{for } x < 0.$$

$$\lim_{x \rightarrow 0} \int_{|x|}^{\infty} \frac{e^{-it}}{t} dt = \frac{\pi}{2}$$

$$\int_{\epsilon}^{\infty} \frac{\cos t}{t} dt = \int_0^{\epsilon} \frac{1 - \cos t}{t} dt + \int_{\epsilon}^{\infty} \frac{\cos t}{t} dt - \int_0^{\epsilon} \frac{1}{t} dt$$

$$\xrightarrow{\beta x \rightarrow +\epsilon} -\frac{\pi i}{2} = \log(\beta|x|) \quad \text{for } x > 0.$$

$$\xrightarrow{\beta x \rightarrow -\epsilon} +\frac{\pi i}{2} = \log(\beta|x|) \quad \text{for } x < 0.$$

$$S_2 = \frac{\gamma}{2\pi} \int_0^{\infty} \left[\frac{k l e^{ikx}}{A} + \frac{k}{B} e^{-ikx} \right] dk$$

$$S_3 = \frac{\gamma}{2\pi i} \int_0^{\infty} \left[\frac{e^{ikx}}{A} - \frac{e^{-ikx}}{B} \right] dk$$

$$\begin{aligned}
 S_2 \xrightarrow{x>0} & \frac{\gamma}{2\pi} \left[\frac{(\alpha-k)}{\alpha+k} \left\{ K \left(-\frac{\pi i}{2} - \log k \alpha \right) - \frac{\alpha^2}{K} \left(-\frac{\pi i}{2} - \log \frac{\alpha^2}{K} \right) \right\} \right. \\
 & \left. + \frac{(\alpha-\beta)}{\alpha+\beta} \left\{ \beta \left(-\frac{\pi i}{2} - \log \beta x \right) - \frac{\alpha^2}{\beta} \left(-\frac{\pi i}{2} - \log \frac{\alpha^2}{\beta} \right) \right\} \right] \\
 & = \frac{\gamma}{2\pi} \left[\frac{\pi}{2i} - \log(\gamma x) \right] \left\{ \frac{\alpha-k}{\alpha+k} \left(K - \frac{\alpha^2}{K} \right) + \frac{\alpha-\beta}{\alpha+\beta} \left(\beta - \frac{\alpha^2}{\beta} \right) \right\} \\
 & + \frac{\gamma}{2\pi} \left[+ \frac{(\alpha-k)}{\alpha+k} \left\{ K \log K - \frac{\alpha^2}{K} \log \frac{\alpha^2}{K} \right\} \right. \\
 & \left. + \frac{(\alpha-\beta)}{\alpha+\beta} \left(\beta \log \beta - \frac{\alpha^2}{\beta} \log \frac{\alpha^2}{\beta} \right) \right]
 \end{aligned}$$

$$\begin{aligned}
 \frac{\alpha-k}{\alpha+k} \left(K - \frac{\alpha^2}{K} \right) + \frac{\alpha-\beta}{\alpha+\beta} \left(\beta - \frac{\alpha^2}{\beta} \right) &= -k(\alpha-k)^2 - \beta(\alpha-\beta)^2 \\
 &= -\gamma + \cancel{\gamma} = 0
 \end{aligned}$$

$$S_2 \xrightarrow{x \rightarrow +0} - \frac{\gamma}{2\pi} \left[\frac{(\alpha-k)}{\alpha+k} \left\{ K \log K - \frac{\alpha^2}{K} \log \frac{\alpha^2}{K} \right\} \right. \\
 \left. + \frac{\alpha-\beta}{\alpha+\beta} \left\{ \beta \log \beta - \frac{\alpha^2}{\beta} \log \frac{\alpha^2}{\beta} \right\} \right]$$

$$\xrightarrow{x \rightarrow -0} - \frac{\gamma}{2\pi} [\text{ " }]$$

$$+ \frac{\gamma}{2i} \left\{ \frac{(\alpha-k)}{\alpha+k} \left(K - \frac{\alpha^2}{K} \right) + \frac{(\alpha-\beta)}{\alpha+\beta} \left(\beta - \frac{\alpha^2}{\beta} \right) \right\}$$

$S_3 \rightarrow$ jump $\frac{\gamma}{2}$
 $\gamma + i\delta //$ jump

$$\left(\frac{\partial}{\partial t} - U \frac{\partial}{\partial x}\right) \phi(x, y, t) = \frac{1}{\pi} \frac{\rho(x, y, t)}{(x-\xi)^2 + y^2} = \frac{1}{\pi} \Pi(x, y, t)$$

$$\Pi(x, y, t) = \frac{1}{\pi} \int_0^t \frac{\rho(\xi, \tau) y d\xi}{(x-\xi)^2 + y^2} \xrightarrow{y \rightarrow 0} \rho(x, t)$$

$$\left(\frac{\partial}{\partial t} - U \frac{\partial}{\partial x}\right) \eta(x, t) = -\phi(x, 0, t)$$

$$\begin{aligned} \left(\frac{\partial}{\partial t} - U \frac{\partial}{\partial x}\right) \phi_y(x, 0, t) &= \Pi_y(x, 0, t) = -\frac{1}{\pi} \int_0^t \frac{\rho(\xi, \tau) d\xi}{(x-\xi)^2} \\ &= \int_0^t \Pi(x + U(t-\tau), y, \tau) d\tau \quad -\tau = \frac{x-\xi}{U} - t \end{aligned}$$

$$\phi(x, y, t) = \frac{1}{U} \int_0^x \Pi(x, y, t + \frac{x-X}{U}) dX + \int_m^x (x + Ut)$$

$X = x + U(t-\tau)$

~~Displacement pot.~~ $\bar{\Phi}$

$$\left(\frac{\partial}{\partial t} - U \frac{\partial}{\partial x}\right) \bar{\Phi}(x, y, t) = \phi(x, y, t)$$

1. $\bar{\Phi}_y(x, 0, t) = -\eta(x, t)$ // $\int_0^x (x + Ut)$

$$\bar{\Phi}(x, y, t) = -\frac{1}{U} \int_0^x \phi(x, y, t + \frac{x-X}{U}) dX + \int_m^x (x + Ut)$$

$X + U(t + \frac{x-X}{U})$

$$\frac{1}{\pi} \int_0^x \frac{\rho(\xi, \tau)}{x-\xi} d\xi = f(x, t)$$

$$\int_0^x \frac{1}{x-\xi} d\xi = \ln(x-\xi)$$

$$\Pi_y(x, t) = f_x(x, t)$$

$$\tau + \frac{x-X}{U} = t$$

$$X = U(t-\tau) + x$$

$$\phi(x, y, t) = \int_0^t \Pi(x + U(t-\tau), y, \tau) d\tau$$

$$I = \frac{1}{\pi} \int_0^c \frac{f(z, t) dz}{x - z}$$

$$\frac{A + Bx + Cx^2}{\sqrt{x(c-x)} \sqrt{x(c-x)}}$$

$$I_n = \frac{(\frac{c}{2})^{2n}}{\pi} \int_0^c \frac{z^n dz}{(x - \frac{z}{3}) \sqrt{3}(c - \frac{z}{3})}$$

$$\begin{cases} x = \frac{c}{2}(1 + \cos \theta), & \frac{c}{2} du = \frac{c}{2} (-\sin \theta) d\theta \\ z = \frac{c}{2}(1 + \cos \theta), & dz = -\frac{c}{2} \sin \theta d\theta \\ \sqrt{3}(c - \frac{z}{3}) = \frac{c}{2} \sin \theta \\ \frac{c}{2} du = \sqrt{\left(\frac{2x}{c}\right)^2 - 1} = \sqrt{\frac{2x}{c}\left(\frac{2x}{c} - 2\right)} \\ = \frac{2}{c} \sqrt{x(x-c)} \end{cases}$$

$$I_n = \frac{(\frac{c}{2})^{2n}}{\pi} \int_0^\pi \frac{(1 + \cos \theta)^n d\theta}{\cos \theta - \cos \theta}$$

$$\frac{1}{\cos \theta - \cos \theta} = \frac{1}{\sin \theta} \sum_{n=0}^{\infty} \epsilon_n e^{-n\theta} \cos n\theta$$

$$I_n = \frac{(\frac{c}{2})^{2n}}{\pi \sin \theta} \sum_{m=0}^{\infty} \epsilon_m e^{-m\theta} \int_0^\pi \cos m\theta (1 + \cos \theta)^n d\theta$$

$$I_0 = \frac{1}{\sin \theta} \rightarrow \frac{1}{i \sin \theta} \quad (1 - 2\cos \theta + \cos^2 \theta) \quad (0 < \theta < \pi)$$

$$I_1 = \frac{1}{\sin \theta} (1 + e^{-i\theta}) \rightarrow \frac{1}{i \sin \theta} (1 + \cos \theta + i \sin \theta)$$

1.

$$I_2 = \frac{1}{\sin \theta} \left(\frac{3}{2} + 2e^{-i\theta} + \frac{1}{2} e^{-2i\theta} \right) \rightarrow \frac{1}{i \sin \theta} \left(\frac{3}{2} + 2\cos \theta + \frac{1}{2} \cos 2\theta - 2i \sin \theta - \frac{1}{2} \sin 2\theta \right)$$

$$I_0 = \frac{c}{2\sqrt{x(x-c)}}$$

$$I_1 = \frac{c}{\sqrt{x(x-c)}} \left(1 + \frac{2x}{c} - \frac{2}{c} \sqrt{x(x-c)} \right)$$

$$= \frac{x}{\sqrt{x(x-c)}} - 1$$

$$I_2 = \frac{c}{2} \frac{(\frac{2x}{c})^2}{\sqrt{x(x-c)}} - 2 - \left(\frac{2x}{c} - 1 \right)$$

$$= \frac{u^2}{\sqrt{u(u-2)}} - u - 1 = \frac{u}{\sqrt{u-2}} - (1+u) = u \left(\frac{1}{\sqrt{u-2}} - 1 \right)$$

$$\phi_{,y} = \int_0^x A L_x(x+u, \tau, 0, \tau) d\tau = \int_0^x A$$

$$L_x = \frac{1}{2\sqrt{x(x-c)}} - \frac{1}{2} \frac{\sqrt{x}}{(x-c)^{3/2}} = \frac{x-c-x}{2\sqrt{x(x-c)}^2}$$

$$x=c(t)$$

$$\phi_{,y} = -\frac{1}{2} \int_0^x \frac{A(c(\tau))}{\sqrt{x+u, \tau} \{x+u, \tau - c(\tau)\}^{3/2}} d\tau$$

$$\eta = -\frac{1}{2} \int_0^x d\tau' \int_0^{\tau'} \frac{A(\tau) c(\tau) d\tau}{\sqrt{x+u, \tau' + u, \tau} \{x+u, \tau' - c(\tau)\}^{3/2}}$$

$$= -\frac{1}{2} \int_0^x \frac{\tau \int_0^{\tau} A(\tau) c(\tau) d\tau}{\tau A} - \int_0^x \frac{\tau A}{\tau A}$$

$$\eta = -\frac{1}{2} \int_0^x \frac{(x-c) A(\tau) c(\tau) d\tau}{\sqrt{x+u, \tau} \{x+u, \tau - c(\tau)\}^{3/2}}$$

1. $c(t) \Rightarrow x = c(t) \text{ at } t$

よおして $\eta(x, t) = \eta_0(t) + \alpha x$

$$= v_0 t + \alpha c(t)$$

$c > x > 0$

$$\eta = -v_0 t + \alpha x \quad \text{for } c(t) > x > 0$$

$$\eta(c(t), t) = -v_0 t + \alpha c(t)$$

定の分明

理論は役に立つか

はいはい

1. 理論とは何か

^{実験}
(実際, 実用)

理論の有用性 (とその分類)

2. 役に立つとはどういう事か

モデルと仮説

定量的 How
定量的
計量的

量的 時空的定量的

有用性とは何か (社会的側面)

難解性

when where
who who

おわりに

事例

研究